# **Parametric Models for Signature Prediction and Feature Extraction**

Julie Ann Jackson

Department of Electrical and Computer Engineering Air Force Institute of Technology, Dayton, OH 45433, USA julie.jackson@afit.edu

*Abstract* — This paper compares and contrasts numerical electromagnetic (EM) prediction methods and parametric scattering models for radar signature prediction and feature extraction.

*Index Terms* – Attributed scattering centers, radar cross section, radar feature extraction, scattering prediction.

# I. INTRODUCTION

Both radar model validation and target recognition applications require accurate, and preferably fast, signature prediction methods, as illustrated in Fig. 1. Prediction methods are nonparametric (e.g., numerical electromagnetic prediction codes) and parametric (e.g., attributed scattering centers). Choice of method should be based on the trade space between model accuracy and computational efficiency. Computational efficiency includes not only the ability to quickly compute the prediction model (the forward problem) but also the complexity and feasibility to extract signatures from measured data (the inverse problem). Numerical electromagnetic (EM) prediction methods are geared toward the forward problem, while parametric models (PMs) have been developed with the inverse problem in mind. The complexity-accuracy trade space for each model type is qualitatively depicted in Fig. 2.

# **II. SIGNATURE PREDICTION**

EM numerical prediction techniques include method of moments (MoM), differential techniques, integral equation solvers, shooting and bouncing rays (SBR) geometric/physical optics (GO/PO), and many other methods, discussed in [1-5]. Computation time varies with the electrical size of the target and is extended by the time it takes to draw/import and facetize/mesh a target model. A method to speed up the EM part of SBR is given in [6], and [7] provides a technique to extend single frequency computations over a band of frequencies. An attempt to speed the drawing portion is provided in [2], which converts a picture into a facet model. Alternatively, [2] lets users build simple targets by combining primitive shapes, which can be characterized by PMs.



Fig. 1. Process flow diagram for signature prediction (forward problem) and signature extraction (inverse problem).



Fig. 2. Scattering models and notional complexity vs. accuracy trade space.

PMs developed for signal processing tasks may also be used for signature prediction. The isotropic point model is characterized by scatterer position and radar cross section (RCS). The isotropic point model is a key assumption in radar imaging; however, realistic scatterer persistence is typically less than 20° [8]. The monostatic 2D attributed scattering center (ASC) model [9] is parameterized by frequency, polarization, aspect (along the length of the target), and length. Other monostatic models include the Huynen and Cameron decompositions that break monostatic polarization responses into primary forms [10-12]. Bistatic canonical shape models parameterized by type, size, and orientation capture 3D physical geometry and model frequency, polarization, and azimuth and elevation aspect dependence [13]. The canonical models are built from products of planar solutions for strip, dihedral, and circular scattering mechanisms [14], [15] to approximate the 3D solution. A full analytic 3D GO/PO solution for bistatic scattering from a dihedral is given in [16]. EM predictions, PMs, and measurements of a dihedral are compared in [17]; PMs took milliseconds to compute, while MoM took hours.

PMs are extremely fast because the equations are written analytically and do not need a numerical solver like EM methods. However, accuracy is limited by underlying GO/PO and planar assumptions; edge diffraction, traveling waves, etc. are not included. Also, the dihedral and trihedral models are defined only within the interior of the corner, though plate models could be combined to model the back sides. Furthermore, PMs do not capture interactions between scatterers. Thus, a major challenge for using PMs for prediction is how to break a complex target into scattering primitives. For example, constructing a vehicle's sides with plates neglects vehicle/ground interaction, which is better modeled with dihedrals.

#### **III. SIGNATURE EXTRACTION**

Numerical EM techniques are not suited to signature extraction since each iteration in an optimization would require update to the facet model and re-run of computationally expensive prediction code. However, as shown in Fig. 1, other feature extraction methods can be used along with model refinement and EM predictions for RCS signature validation.

Parametric methods were developed with signal estimation techniques and target recognition applications in mind. Parameters may be estimated from measured data, though estimation complexity increases with model complexity. Isotropic points may be estimated using the CLEAN algorithm [18], [19]. Two-dimensional ASCs may be estimated using Prony's method or matrix pencil method [9]. Canonical shape primitives are more difficult to extract since shape selection and parameter estimation are coupled; however, an initial iterative approach is given in [20]. Other approaches to parametric model extraction include Expectation-Maximization [21], sparse dictionary techniques [22-24], and ray-tracing methods [19], [25]. Limited data from practical radar flight paths complicates the classification and estimation problem, as illustrated in [26], since objects may look similar for a narrow-angle data slice.

## **IV. CONCLUSION**

We have provided an overview of numerical EM prediction versus PMs. While PMs are limited to simple scattering mechanisms, they are fast and well-suited to signature extraction. Numerical EM codes enable high fidelity prediction of complex targets; however, it is not computationally feasible to use EM methods for signature extraction. Thus, one should choose a signature prediction method depending on the application.

## ACKNOWLEDGMENT

The views expressed in this article are those of the authors and do not reflect the official policy or position of the U.S. Air Force, Department of Defense, or the U.S. Government. Approved for public release #88ABW-2017-4831.

#### REFERENCES

- C. Uluisik, et al., "Radar cross section (RCS) modeling and simulation, Part 1: A tutorial review of definitions, strategies, and canonical examples," *IEEE Antennas Propag. Mag.*, vol. 50, no. 1, pp. 115-126, Feb. 2008.
- [2] G. Cakir, M. Cakir, and L. Sevgi, "Radar cross section (RCS) modeling and simulation, Part 2: A novel FDTD-based RCS prediction virtual tool for the resonance regime," *IEEE Antennas Propag. Mag.*, vol. 50, no. 2, pp. 81-94, Apr. 2008.
- [3] A. K. Bhattacharyya and D. L. Sengupta, *Radar Cross Section Analysis and Control*. Boston: Artech House, 1991.
- [4] W. C. Chew, et al., "Fast solution methods in electromagnetics," *IEEE Trans. on Antennas Propag.*, vol. 45, no. 3, pp. 533-543, Mar. 1997.
- [5] J. Song, C.-C. Lu, and W. C. Chew, "Multilevel fast multipole algorithm for electromagnetic scattering by large complex objects," *IEEE Trans. on Antennas Propag.*, vol. 45, no. 10, pp. 1488-1493, Oct. 1997.
- [6] R. Bhalla and H. Ling, "A fast algorithm for signature prediction and image formation using the shooting and bouncing ray technique," *IEEE Trans. on Antennas Propag.*, vol. 43, no. 7, pp. 727-731, July 1995.
- [7] C. J. Reddy, et al., "Fast RCS computation over a frequency band using method of moments in conjunction with asymptotic waveform evaluation technique," *IEEE Trans. on Antennas Propag.*, vol.

46, no. 8, pp. 1229-1233, Aug. 1998.

- [8] D. E. Dudgeon, R. T. Lacoss, C. H. Lazott, and J. G. Verly, "Use of persistent scatterers for modelbased recognition," in *Proc. SPIE*, vol. 2230, pp. 2230-2230-13, 1994.
- [9] L. C. Potter and R. L. Moses, "Attributed scattering centers for SAR ATR," *IEEE Trans. Image Process.*, vol. 6, no. 1, pp. 79-91, Jan. 1997.
- [10] J. R. Huynen, "Phenomenological theory of radar targets," in *Electromagnetic Scattering*, P. L. E. Uslenghi, Ed. Academic Press, 1978.
- [11] W. L. Cameron, "Feature motivated polarization scattering matrix decomposition," in *Record of the IEEE 1990 Int'l Radar Conference*, May 1990, pp. 549-557.
- [12] S. R. Cloude and E. Pottier, "A reveiw of target decomposition theorems in radar polarimetry," *IEEE Trans. Geosci. Remote Sens.*, vol. 34, no. 2, pp. 498-518, Mar. 1996.
- [13] J. A. Jackson, B. D. Rigling, and R. L. Moses, "Canonical scattering feature models for 3D and bistatic SAR," *IEEE Trans. Aerosp. Electron. Syst.*, vol. 46, no. 2, pp. 525-541, Apr. 2010.
- [14] M. Gerry, "Two-Dimensional Inverse Scattering Based on the GTD Model," The Ohio State University: Ph.D. Dissertation, 1997.
- [15] N. Akhter, "Far Zone Electromagnetic Scattering From Complex Shapes Using Geometrical Theory of Diffraction," The Ohio State University: Ph.D. Dissertation, 1993.
- [16] J. A. Jackson, "Analytic physical optics solution for bistatic, 3D scattering from a dihedral corner reflector," *IEEE Trans. on Antennas Propag.*, vol. 60, no. 3, pp. 1486-1495, Mar. 2012.
- [17] A. Tempelis, M. Jussaume, and J. Jackson, "Comparison of measured and predicted bistatic scattering from a right-angle dihedral," in *IEEE Radar Conference*, May 2011, pp. 135-140.
- [18] J. A. Hogbom, "Aperture synthesis with a nonregular distribution of interferometer baselines," *Astronomy and Astrophysics Supplement Series* (0365-0138), vol. 15, no. 3, pp. 417-426, 1974.
- [19] R. Bhalla and H. Ling, "Three-dimensional scattering center extraction using the shooting and bouncing ray technique," *IEEE Trans. On Antennas Propag.*, vol. 44, no. 11, pp. 1445-1453, Nov. 1996.
- [20] J. Jackson and R. Moses, "Synthetic aperture radar 3D feature extraction for arbitrary flight paths," *IEEE Trans. Aerosp. Electron. Syst.*, vol. 48, no. 3, pp. 2065-2084, July 2012.
- [21] J. A. Richards, A. S. Willsky, and J. W. Fisher III, "Expectation maximization approach to target model generation from multiple synthetic aperture radar images," *Optical Engineering*, vol. 41, no. 1, pp. 150-166, Jan. 2002.

- [22] K. R. Varshney, M. Cetin, J. W. Fisher, and A. S. Willsky, "Sparse representation in structured dictionaries with application to synthetic aperture radar," *IEEE Trans. Signal Process.*, vol. 56, no. 8, pp. 3548-3561, Aug. 2008.
- [23] G. B. Hammond and J. A. Jackson, "Canonical feature extraction using molecule dictionaries," in *IEEE Radar Conference*, paper 5092, pp. 1-6, 29 Apr.-3 May 2013.
- [24] H. Liu, et al., "Attributed scattering center extraction algorithm based on sparse representation with dictionary refinement," *IEEE Trans. On Antennas Propag.*, vol. 65, no. 5, pp. 2604-2614, May 2017.
- [25] Y. He, et al., "A forward approach to establish parametric scattering center models for known complex radar targets applied to SAR ATR," *IEEE Trans. on Antennas Propag.*, vol. 62, no. 12, pp. 6192-6205, Dec. 2014.
- [26] J. A. Jackson and R. L. Moses, "Identifiability of 3D attributed scattering features from sparse nonlinear apertures," in *Proc. SPIE*, vol. 6568, 2007, pp. 6568-6568-12.



Julie Ann Jackson is an Associate Professor of Electrical Engineering at the Air Force Institute of Technology (AFIT), where she joined the faculty in 2009. She earned the B.S.E.E. degree from Wright State University, Dayton, OH, in 2002 and the M.S. and Ph.D.

degrees from The Ohio State University, Columbus, OH, in 2004 and 2009, respectively. Her graduate studies were funded with fellowships from the National Science Foundation, the Dayton Area Graduate Studies Institute, The Ohio State University, and the Ohio Board of Regents. Jackson has held internships at the Air Force Research Laboratory, Alphatech, Inc., Jacobs Sverdrup, and Bell Laboratories. She is a Senior Member of the IEEE, Member of Eta Kappa Nu and Tau Beta Pi, and Chief Advisor for the Ohio Eta Chapter of Tau Beta Pi. Jackson was elected in 2018 to the IEEE AES Society Radar Systems Panel and serves on the technical program committees of the IEEE Radar Conference and the MSS Tri-Service Radar Conference. Jackson's contributions have been recognized with multiple awards including the Air University Civilian Quarterly Award in 2018, the Southwestern Ohio Council for Higher Education (SOCHE) 2016 Faculty Excellence Award, and the 2012 Air Force Science, Technology, Engineering, and Mathematics Award for Outstanding Scientist/Engineer, Junior Civilian. Her research interests are in radar signal processing and imaging and exploitation of RF signals.