Temperature Effects Analysis on Microwave Rectifiers by Field-Circuit Hybrid Multiphysics Simulation

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Abstract - This work analyzes the temperature effects on microwave circuits by employing a novel field-circuit hybrid multiphysics simulation. Firstly, the multiphysics simulation is implemented by solving the coupled governing equations including Poisson equations, semiconductor transport equations, and thermodynamic equations; then, the multiphysics simulation is incorporated into circuit analysis; finally, the circuit simulation results are integrated into the finite-difference timedomain (FDTD) simulation by equivalent sources. In this manner, a field-circuit hybrid multiphysics simulation method is presented. Taking two different microwave rectifiers operating at S- and C-band as examples, temperature effects are analyzed by the proposed approach. Simulation results are in good agreement with measured values, demonstrating the accuracy and applicability of the proposed approach. The presented method more suitably reveals the temperature effects on the rectifier.

Index Terms – field-circuit hybrid simulation, multiphysics, Schottky diode rectifier, temperature effects.

I. INTRODUCTION

It is well known that temperature has a major impact on the performance of semiconductor devices and circuits. This is attributable to the fact that temperature changes the effective carrier density, electron and hole mobility, and material properties of semiconductor devices, thereby affecting the performance of the entire circuit [1].

With the development of wireless power transmission, research on microwave rectifiers has attracted considerable attention as a key component of converting space electromagnetic energy into DC. Thereby, the temperature effects caused by the injection of high-power microwave energy into the rectifier cannot be ignored. The accurate and efficient simulation of the temperature effects requires solving more challenging multiphysics problems [1–3]. Currently, multiphysics simulation of semiconductor devices has become a reality. Since multiphysics simulation can better describe the operation of semiconductor devices under various conditions and more accurately predict their physical effects, the multiphysics analysis of semiconductor devices and circuits has received increasing attention in recent years [2]. Abundant research on the electrothermal behaviors of semiconductor devices and circuits, characterized by combining multiple physical equations including electromagnetic fields, semiconductor transport, and thermodynamics, is already available [3-6]. However, the multiphysics simulation of semiconductor devices is very complicated and time-consuming. Considering the significant time and memory requirement, even for the nextgeneration computer systems, it is almost impossible to accomplish the temperature analysis of entire microwave circuits [7].

So far, research works on temperature effect simulation of the whole microwave circuit are very rare. In general, microwave circuits could be analyzed using either frequency- or time-domain full-wave simulation method [8]. However, in dealing with nonlinear semiconductor devices, time-domain methods enjoy the advantage of allowing for the direct analysis of field-circuit interactions without resorting to harmonic balance or port extraction methods [9]. Since FDTD method remains a popular choice for solving many electromagnetic problems, because of its versatility and ability for dealing with complex geometries, materials, and environments [10–12]. Thus, in the authors' previous work, a physical model-based field-circuit hybrid simulation method was proposed, and a good agreement between rectifier simulation and measurements was obtained. However, the temperature effects on the microwave rectifier were not taken into account in order to simplify the simulation process [13]. Since microwave rectifiers usually work under high frequency and/or large signals, the temperature effects cannot be ignored. Therefore, the presented research extends previous work by coupling the multiphysics simulation of semiconductor devices to fieldcircuit hybrid simulation based on FDTD. To this end, the multiphysics simulation is implemented by solving the coupled governing equations including Poisson equations, semiconductor transport equations, and thermodynamic equations; then the multiphysics simulation is incorporated into circuit analysis; finally, the circuit simulation taking into account multiphysics is coupled to FDTD simulation by equivalent sources. In this manner, this paper presents a hybrid field-circuit multiphysics simulation approach. The presented simulation approach is applied to analyze the temperature effects of microwave rectifiers operating at S- and C-band frequencies and a series of experiments are conducted to validate the approach.

This approach not only characters the behaviors of microwave rectifiers under large signal conditions but also predicts its temperature effects. A further obvious advantage is that the hybrid solution scheme reduces the computational burden significantly, enabling systemlevel circuit simulation and analysis of temperature effects.

II. THE HYBRID FIELD-CIRCUIT SIMULATION APPROACH BASED ON MULTIPHYSICS

The size of semiconductor chips is on the microor nano-scale, while the size of device packages and microwave circuits may be on the millimeter scale or larger. Assuming the FDTD field-circuit simulation adopts the unified grid discretization, then the required calculations resources are prohibitively large to accomplish the simulation. While the field-circuit simulation based on an equivalent source can easily integrate the equivalent circuits simulation into full-wave FDTD simulation, greatly reducing the computational burden. Therefore, in order to address the temperature effect analysis problem of microwave rectifiers, this paper couple multiphysics simulation of the semiconductor device to the circuit simulation, and integrate them into the FDTD simulation by equivalent sources, presenting a more accurate and effective hybrid simulation approach. This section provides an introduction to the multiphysics simulation of semiconductor devices and their coupling with circuits, as well as the field-circuit hybrid multiphysics simulation based on equivalent sources.

A. Multiphysics analysis and simulation for semiconductor devices

The physical model of semiconductor devices is established based on the geometrical structure and manufacturing process and represented by parameters such as the device's junction width, gate length, channel thickness, etc. Semiconductor devices are often thermally sensitive, and multiphysics simulations that include temperature effects more accurately model carrier transport and characterize device behaviors.

For numerical analysis of semiconductor devices, a series of low-order approximate equations can be derived from electromagnetic field theory and semiconductor physics. Among them, the drift-diffusion model (DDM) is the most widely used semi-classical model. Up until now, DDM successfully simulate the semiconductor carrier transport phenomenon under non-isothermal conditions, thereby basic equations are Poisson Equation, current continuity equation, and drift-diffusion equation [14, 15]:

$$\varepsilon \nabla^2 \varphi = q \left(p - n + N_t \right), \tag{1}$$

$$\partial n/\partial t = q^{-1} \nabla J_n + G - R, \qquad (2)$$

$$\partial p/\partial t = -q^{-1}\nabla J_p + G - R,$$
 (3)

$$J_n = \mu_n k_B (T \nabla n + n \nabla T) + q \mu_n n \nabla \varphi, \qquad (4)$$

$$J_p = -\mu_p k_B (T\nabla p + p\nabla T) + q\mu_p p\nabla \varphi, \qquad (5)$$

where ε , q and φ denote the material permittivity, electronic chargeand electrostaticpotential, respectively; N_t , n and p denote the doping, electron and holes density, respectively. G and R denote carriers generation rate and recombination rate, respectively. J_n and J_p denote the electron and the hole current density, respectively; T, k_B , μ_n and μ_p denote the temperature, Boltzmann constant, electron and hole mobility, respectively [1].

To analyze the temperature effects on semiconductor performance in microwave power circuits, in addition to DDM, the multiphysics simulation of semiconductor devices should contain the heat conduction equation and equations containing temperature-dependent characteristic parameters [16]:

$$\rho c \cdot \partial T / \partial t = \nabla [k(T)\nabla T] + g, \tag{6}$$

$$g = (J_n + J_p + \varepsilon \partial E / \partial t) \cdot E + RE_g, \tag{7}$$

$$n_i^2 = n_0 p_0 = N_c N_v \exp(E_g/k_B T),$$
 (8)

$$\mu_{n,p}(T) = \mu_{n,p}^{0} \left(T/T_0 \right)^{-\alpha} / \left[1 + (E/E_c)^{\beta} \right]^{1/p}, \quad (9)$$

$$\tau_{n,p}(T) = \tau_{n,p}^0 \left(1 + N_t / N_{n,p} \right) (T/T_0)^r, \quad (10)$$

where ρ and *c* are the material density and the thermal conductivity, respectively; *g* is the heat generated per unit time and volume, *E* and *E_g* is the electric field and band-gap width of diode, respectively; *N_c* and *N_v* are effective state densities of the conduction band bottom and valence band top, respectively; $\mu_{n,p}^0$ and $\tau_{n,p}^0$ are the effective mobility and the lifetime of electrons and holes at ambient temperature, respectively; E_c is the critical field;; α, β and γ are empirical constant [14].

The multiphysics equation system consists of Eqs. (1)–(10) and is a coupled nonlinear partial differential equation system. In fact, it is impossible to give a closed-form solution, thereby an iterative numerical method is employed to solve this system equations.

It can be seen that the main unknowns in the multiphysics equation system are: n, p, φ and T. Without loss of generality, taking one-dimensional space x = 0 - L as an example, the device grid division is shown in Fig. 1.

$$\begin{array}{c|c} & \stackrel{h'(k)}{\longleftarrow} & \stackrel{h'(k+1)}{\longleftarrow} & \stackrel{h'(k+2)}{\longleftarrow} \\ & \stackrel{1}{\longleftarrow} & \stackrel{k-1}{\longleftarrow} & \stackrel{k}{\longleftarrow} & \stackrel{k+1}{\longleftarrow} & \stackrel{k+2}{\longleftarrow} \\ & \stackrel{1}{\longleftarrow} & \stackrel{1}{\longleftarrow} & \stackrel{k+1}{\longleftarrow} & \stackrel{k+2}{\longleftarrow} & \stackrel{N}{\longleftarrow} \\ & x = 0 & M-1 & M & M+1 & M+2 & x = L \\ & \stackrel{1}{\longleftarrow} & \stackrel{1}{\longrightarrow} & \stackrel{1$$

Fig. 1. The one-dimensional difference grids of semiconductor devices.

When *T* is a known value, The electrical characteristics Eqs. (1)–(5) are discretized by central difference and linearize [17], the whole procedure can be simplified to the solution of an increment equation [18]:

$$A\Delta y_{k-1} + B\Delta y_k + C\Delta y_{k+1} = H_k, \tag{11}$$

where 3×3 coefficient matrices; H is a 3×1 coefficient matrices. coefficient matrices value are described in [16].

When n, p and φ are known values, the heat conduction Eq. (6) may be discretized into first-order ordinary time-dependent differential equations [18]:

$$\frac{T_{k+1} - T_k}{h_{k,k+1}} - \frac{T_k - T_{k-1}}{h_{k-1,k}} + g = \frac{dC_k \cdot T_k}{dt}, \quad (12)$$

where C_k , $h_{k,k+1}$ and $h_{k-1,k}$ are the discretization coefficients. By using the Newton-Raphson iteration method,(12) can be can be rewritten as an increment equation:

$$aT_{k-1} + bT_k + cT_{k+1} = h, (13)$$

where a, b, c, and h are the coefficients. Eqs. (11) and (13) can also be solved by using the chasing method, and the true values of n, p, φ , and T can be obtained after many iterations [19].

The iterative procedure for the multiphysics simulation of the semiconductor model is shown in Fig. 2. Firstly, the physical parameters of the semiconductor device are calculated by the initial electrical and temperature parameter (the carrier mobility generation and recombination rate etc.) and the semiconductor devices are solved by introduced electrical Eqs. (1)-(5). Then the heat conduction Eq. (6) and (7) are solved by the electric field, current, and other parameters to obtain the temperature, the electrical parameters are updated based on the current temperature and obtain the electrical field and temperature until it converges. Finally, the device voltage and current is calculated.



Fig. 2. Brief flow chart for multiphysics simulation of semiconductor device.

B. Integrating multiphysics simulation of semiconductor devices into circuit analysis

The circuit analysis is an indispensable part for conventional field-circuit hybrid simulation, which needs to integrate the equivalent circuit simulation into FDTD by equivalent sources. According to circuit analysis theory, circuit simulation can be rewritten as a system of equations by an improved nodal analysis method [20]:

$$\begin{cases} f_1(U_1, U_2, \dots, U_k) = 0\\ f_2(U_1, U_2, \dots, U_k) = 0\\ \dots\\ f_k(U_1, U_2, \dots, U_k) = 0 \end{cases}$$
(14)

Here k is the index of the unknown node voltage, U is the unknown value, $f_k(U_1, U_2, ..., U_k)$ is the node voltage equation. The solution procedure of the nonlinear(14) is converted to the Newton-Raphson iterative equations:

$$U^{n+1} = U^n - J^{-1}(U^n) f(U^n),$$
(15)

where
$$U = [U_1, U_2, ..., U_k]^T$$
, $f(U) = [f(U_1), f(U_2), ..., f(U_k)]^T$.

 $J_{\rm is}$ the node voltage equation:

$$J = \begin{bmatrix} \frac{\partial f_1}{\partial U_1} & \frac{\partial f_1}{\partial U_2} & \cdots & \frac{\partial f_1}{\partial U_k} \\ \frac{\partial f_2}{\partial U_1} & \frac{\partial f_2}{\partial U_2} & \cdots & \frac{\partial f_2}{\partial U_k} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f_k}{\partial U_1} & \frac{\partial f_k}{\partial U_2} & \cdots & \frac{\partial f_k}{\partial U_k} \end{bmatrix}$$
(16)

For any semiconductor device in the circuit, assuming the device is located in the j-th branch, and two adjacent nodes are (k-1) and k, the nonlinear relationship between the branch current I_j and the terminal voltage can be expressed as [20]:

$$I_j = \psi(U_j) = \psi(U_k, U_{k-1}).$$
 (17)

To obtain transient response of the circuit, the diode branch current Eq. (17) is obtained by the multiphysics simulation, introduced previously. while the branch currents of other linear devices are derived from the circuit simulation based on its constitutive equations. In this way, the multiphysics and the circuit simulation are integrated into a unified scheme.

C. Field-circuit hybrid multiphysics simulation based on equivalent sources

In numerical simulation of antennas and microwave circuits based on FDTD, the current through the lumped element can be regarded as an additional current term in the Maxwell's integral equations [21]:

$$\oint_C \overrightarrow{E} \cdot d\overrightarrow{l} = -u \int_S \frac{\partial \overrightarrow{H}}{\partial t} \cdot d\overrightarrow{s}.$$
 (18)

$$\oint_{C} \overrightarrow{H} \cdot d\overrightarrow{l} = \varepsilon \int_{S} \frac{\partial \overrightarrow{E}}{\partial t} \cdot d\overrightarrow{s} + I_{s}, \qquad (19)$$

where I_s represents the current flowing through the semiconductor device. The Eqs. (18) and (19) can be easily convert to differential forms, and discrete by FDTD Yee grid. Since physical sizes of semiconductor devices are generally much smaller than the minimum wavelength of the operating frequency, it could be modeled by one dimension, and only occupied one or several serial Yee grid under the uniform FDTD framework, as shown in Fig. 3.

Without loss of generality, in Fig. 3, assume a semiconductor device is located between nodes a and b,



Fig. 3. Discrete form of Yee grid containing semiconductor devices.

The terminal voltage of the semiconductor device V_{ab} can easily be derived from the electric field through path integral [21]:

$$V_{ab}^n = \int_a^b \vec{E}_{ab}^n \cdot d \ \vec{l}.$$
 (20)

A control equation can be derived by combining with Eqs. (18)-(20):

$$(I_x^{n+1})_{EM} = \frac{V_{ab}^{n+1}}{(R_x^{n+1})_{grid}} + I_{sx}^{n+1}.$$
 (21)

In which [21]:

$$(I_x^{n+1})_{EM} = \frac{\sum_{\beta=(i_k, j_s, k_b)}^{\beta=(i_k, j_s, k_b)} dx \cdot \mathbf{K}_{xijk}^{n+1}}{(R_x^{n+1})_{grid}}.$$
 (22)

$$\left(R_x^{n+1}\right)_{grid} = \sum_{\beta=(i_i, j_a, k_a)}^{\beta=(i_0, k_k, k_j)} \frac{\Delta t}{\varepsilon_{x(i, j, k)}} \cdot \frac{\Delta x}{\Delta y \cdot \Delta z}.$$
(23)

$$K_{xijk}^{n+1} = E_{x(i,j,k)}^{n} + \frac{dt}{\varepsilon} \left(\frac{H_{z(i,j,k)}^{n+\frac{1}{2}} - H_{z(i,j-1,k)}^{n+\frac{1}{2}}}{dy} - \frac{H_{y(i,j,k)}^{n+\frac{1}{2}} - H_{z(i,j,k-1)}^{n+\frac{1}{2}}}{dy} - J^{n+\frac{1}{2}}_{cx(i,j,k)} \right). \quad (24)$$

According to circuit analysis, the form of Eq. (21) can be interpreted as a controlled current source in parallel with an equivalent resistance. Where I_{EM} is deduced from the electromagnetic field value of the previous time step, R_{grid} is an equivalent resistance that calculated from FDTD grid size [21]. The FDTD field-circuit scheme along the y, z direction is similar, its implicit form ensures simultaneous calculation of the electric field (deduced from voltage) and current, resulting in the simulation method having a higher stability.

Microwave circuits containing semiconductor devices are generally considered to be a hybrid system and can be simulated using a field-circuit hybrid method based on equivalent sources [22]. Generally, the equivalent sources first equate the electromagnetic field effect on the semiconductor devices as lumped circuits, and then solves the circuits formed by the connection between the equivalent source and the lumped circuit, finally converting the obtained voltage or current to the electric or magnetic field value.

In our proposed field-circuit hybrid multiphysics simulation method, the equivalent circuits of semiconductor devices are substituted by multiphysics modeling and simulation; then, the multiphysics simulation of semiconductor devices is coupled with circuit analysis, and integrate into FDTD full-wave simulation. The transient simulation of the entire circuit system is implemented by advancing synchronously and exchanging data within each FDTD time step, as shown in Fig. 4.

It is important to emphasize that the initial state of the circuit transient analysis needs to be set to the end



Fig. 4. The coupling relationship of multi-physics field.



Fig. 5. The flow chart of field-circuit hybrid multiphysics Simulation.

state, especially the state of the semiconductor device (including electric field, carrier density distribution, and mobilities, temperature, etc.) at the previous time step. This is especially essential for accurate and effective analysis of the whole system. A brief flow chart is shown in Fig. 5.

III. SIMULATION AND EXPERIMENT

Silicon-based diodes of the HSMS-282x series are widely used in microwave rectifiers, featuring low costs and good RF characteristics. It is composed of thin epitaxial layers deposited on heavily doped substrates, with



Fig. 6. Physical model parameters of Schottky diodes: (a) the structure of Schottky diode, (b) the package equivalent circuit.

Schottky contacts at the anode and ohmic contacts at the cathode [13].

To reduce the simulation burden, we make a onedimensional simplification with maintaining the diode characteristics, and its inner structure is shown in Fig. 6 (a) [23]. In this figure, Schottky barrier height and metal work function are denoted by ϕ_B and ϕ_M , respectively; the doping concentration of epitaxial layer and substrate are indicated by $N_d N_D$ and N_{sub} , respectively; the length of epitaxial layer and substrate are indicated by $L_E L_{epi}$ and L_{sub} , respectively L_{sub} ; the effective contact area of the diode is denoted by A_d . For microwave frequency applications, the diode package effect cannot be ignored. Schottky diodes of HSMS-282x series adopt SOT-323 package size, the package effect could be characterized by the equivalent circuit shown in Fig. 6 (b), which is suitable up to 6 GHz. In Fig. 6 (b), C_{L1} and C_{L2} are lead capacitors, respectively; C_p is the package capacitor; Lbond and Llead are the welding inductance and lead inductance, respectively.

The physical model and package parameters of Schottky diode HSMS-282 and HSMS-286 have been extracted in the authors' previous work, they are listed in Table 1 and Table 2 respectively for easy reference [13].

The MW-to-DC power conversion efficiency (PCE) is a key indicator to measure the performance of microwave rectifiers [24]. Generally, PCE of the rectifier could be calculated by the following formula:

$$\eta = \frac{P_{DC}}{P_{MV}} \cdot 100\% = \frac{V_{\text{out}}^2}{P_{MV} \cdot R_{\text{load}}} \cdot 100\%, \quad (25)$$

where P_{MV} and P_{DC} are the microwave input Power and DC output power, respectively; V_{out} and R_{load} are the output DC voltage and load, respectively [24].

To verify the accuracy and applicability of the proposed method in simulating the temperature effects of

Parameters	HSMS-282	HSMS-286
Φ_B [V]	0.629	0.568
Φ_M [V]	4.679	4.631
$N_d [{\rm m}^{-3}]$	5.44×10^{14}	2.91×10^{16}
$N_{sub} [m^{-3}]$	2×10^{18}	2×10^{18}
L_{epi} [μ m]	0.97	1.327
L_{sub} [μ m]	1.02	1.33
$A_d [\mathrm{cm}^2]$	6×10^{-6}	5.61×10^{-6}

Table 1: Physical parameters of two Schottky diodes

Table 2: Package parameters of two Schottky diodes

Parameters	HSMS-282	HSMS-286
C_p [pF]	0.16	0.2
Lbond [nH]	0.79	0.525
L _{lead} [nH]	0.86	0.98
$C_{L1}[pF]$	0.007	0.02
<i>C</i> _{<i>L</i>2} [pF]	0.002	0.08

microwave circuit, taking two different microwave rectifiers operating at S- and C-band as examples, the simulations are performed by presenting a field-circuit hybrid multiphysics approach under different ambient temperatures (25 °C, 75 °C). The simulation program is executed on a computer workstation with a 3.4GHz frequency Intel Core CPU, 32GB memory and 64-bit Windows operating system. Furthermore, two rectifiers are placed into a well-sealed thermostat, and the conversion efficiency is measured to validate the simulation results.

A. The temperature effects analysis on S-band microwave rectifiers

A compact S-band microwave rectifier working at a frequency of 2.45 GHz has been manufactured by utilizing the HSMS-282B diode. The type of printed circuit board (PCB) used in the rectifier is F4B-2 with a relative dielectric constant of 2.65, a loss tangent of 0.0012 and a thickness of 1 mm. The manufactured rectifier dimension is 20 mm \times 16 mm; its structure and photograph are shown in Fig. 7 (a) and (b), respectively.

It is known that the rectifier performance is determined by the entire circuit structures, including input matching and output filtering. However, as a nonlinear device, the Schottky rectifier diodes always generate high-order harmonics. Although the output filters only allow DC to pass through and reflects the fundamental frequency and harmonics, there are still a few harmonics superimposed on the DC output to cause a ripple.

For the S-band rectifier, the computational domain is uniformly divided into $240 \times 190 \times 32$ (including 5-layer air and 10-layer CPML) grids in the x, y, and z directions, the number of iterations is 55000, each iteration



Fig. 7. (a) Schematic diagram of the 2. 45 GHz rectifier; (b) Photograph of manufactured 2. 45 GHz rectifier.



Fig. 8. Several typical output voltages of S-band rectifier at different ambient temperatures.



Fig. 9. PCE of S-band rectifier simulation and measurements at different ambient temperatures.

time is approximately 8.4 s, the total simulation time is about 128.3 hours. Here, several typical simulated output voltages of the rectifier at different ambient temperatures are given in Fig. 8. The simulated and measured PCE under different temperature (25 °C, 75 °C) are shown in Fig. 9.

B. The temperature effects analysis on C-band microwave rectifiers

A C-band rectifier was manufactured working at frequency 5.8 GHz by utilizing the HSMS-286B diode, which still adopts the same PCB as the above-mentioned S-band microwave rectifier. The manufactured rectifier dimension is 20 mm \times 30 mm, its structure and photograph are shown in Fig. 10 (a) and (b), respectively.



Fig. 10. (a) Schematic diagram of the 5. 8 GHz rectifier; (b) Photograph of manufactured 5. 8 GHz rectifier.

For the C-band rectifier, the computational domain is uniformly divided into $280 \times 280 \times 22$ (including 5layer air and 10-layer CPML) grids in the x, y, and z directions, the number of iterations is 35000, each iteration step is approximately 9.6 s, the total simulation time is about 93.3 hours. The typical output voltages of Cband rectifier at different ambient temperatures (25 °C, 75 °C) are simulated, and shown in Fig. 11. The simulated and measured PCE under different temperature are shown in Fig. 12.

From Figs. 9 and 12, it can be clearly seen that both S-band and C-band Schottky rectifiers, the PCE have a consistent variation trend with temperature. The slight errors may attribute to the discontinuities of SMA



Fig. 11. Several typical output voltages of C-band rectifier at different ambient temperatures.



Fig. 12. PCE of C-band rectifier simulation and measurements at different ambient temperatures.

connectors and temperature effects on PCB material properties. The PCE increases slightly with temperature increase under low input power, yet decreases significantly with temperature increase under high input power. From a physical point of view, that is due to the fact that the Schottky diode is a cut-off state under low input power, carrier density of the Schottky diode increase with temperature rise, which causes diode current aggrandize and makes the PCE gradually increase. However, as the input power continually increases, the Schottky diode becomes a turn-on state, the diode impedance diminution with the temperature rise, which will lead to the input and output impedance mismatch and make the PCE decrease significantly.

The measured results are validated by the simulation results at different temperatures, which confirm the effectiveness and applicability of our proposed approach.

Furthermore, excessive input power may cause Schottky diode self-heating, resulting in power conversion efficiency decrease. Thus, power conversion efficiency of rectifiers can be optimized by carefully selecting suitable temperature conditions, especially for energy harvesting application at a low input power level.

IV. CONCULSION

The temperature effects of electronic devices and circuits are essential for microwave power application. This paper adopts a novel field-circuit hybrid multiphysics simulation to analyse the temperature effects of microwave rectifier. Firstly, multiphysics model involving semiconductor and thermal conducting is solved; then, multiphysics simulation is embedded into circuit analysis; finally, this circuit analysis was coupled into field-circuit hybrid simulation based on FDTD. Taking two different Schottky diode rectifiers operating at S- and C-band as examples, simulation results match well with the measured ones, which validate the accuracy and applicability. This method that combines the multiphysics simulation and FDTD solution can greatly improve the simulation accuracy of microwave power circuits. This approach not only has the advantage of accuracy and versatility stemming from the multiphysics simulation, but also retains simplicity and efficiency of the FDTD field-circuit hybrid simulation.

Moreover, the propose method effectively reveal the physical mechanism of rectifier temperature effects. Furthermore, the presented approach could be extended to more complex circuits without significant modifications. This method may become an attractive candidate for simulating and predicting temperature effects of microwave power circuits.

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