# Low-loss Miniaturized Tri-band Bandpass Filter with High Selectivity and Good Passband Symmetry

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**Abstract** -This paper introduces a low-loss microstrip line tri-band bandpass filter, utilizing quarter-wavelength  $(\lambda_g/4)$  tri-section stepped impedance resonators (TSSIRs). In this design, the adoption of a non-edgecoupled structure effectively eliminates the presence of coupling gaps. As a result, additional radiation losses are avoided, leading to lower insertion loss. In addition, the operating frequencies of the three passbands can be flexibly adjusted by tuning the impedance ratios in the TSSIR. Moreover, the  $\lambda_g/4$  TSSIR exhibits a smaller size compared to existing  $\lambda_g/2$  TSSIRs, resulting in a more compact overall design. In order to validate the proposed design methodology, a tri-band bandpass filter with passbands centered at 1.0 GHz, 3.5 GHz, and 6.0 GHz was designed, fabricated, and measured. The minimum insertion losses for each passband were measured to be 0.07 dB, 0.52 dB, and 1.14 dB, respectively. The filter occupies a compact area of  $31 \times 21.5 \text{ mm}^2$  (0.17 $\lambda_g \times 0.12\lambda_g$ ), demonstrating excellent passband symmetry for each frequency band. The proposed tri-band bandpass filter not only achieves three desirable operating frequencies but also benefits from the inherent characteristics of conventional filters, such as remarkably low insertion loss and good passband symmetry.

*Index Terms* – Bandpass filters, high selectivity, low-loss feature, passband symmetry, TSSIRs.

## I. INTRODUCTION

In recent years, multiband and multi-standard wireless communication systems have garnered significant attention due to their ability to support diverse communication standards and frequency bands [1]–[3]. Multiband bandpass filters are essential passive components in these systems, significantly influencing overall performance. Consequently, extensive research has been conducted to develop various design approaches for multiband bandpass filters. Traditional tri-band band-

pass filters have been realized using three sets of resonators with common feeds [4]. However, these designs often suffer from large footprints due to the extensive use of resonators. To address this issue, alternative methods have been proposed, such as employing two sets of resonators where one set operates at two frequencies [5]–[6]. Another approach involves half-wavelength tri-section stepped impedance resonators ( $\lambda_g/2$  TSSIRs,  $\lambda_g$  is the guided wavelength at the center frequency of the first passband) and other multi-mode resonators which can achieve tri-band functionality with only one set of resonators. Despite these innovations,  $\lambda_g/2$  TSSIRs and multi-mode resonators still occupy a relatively large area [7]-[11]. Additionally, since the aforementioned filters all employ an edge-coupled structure, the coupling gaps are prone to generating certain levels of radiation. This radiation effect inevitably leads to relatively high insertion losses in these structures. Substrate integrated waveguide (SIW) has emerged as a widely adopted low-loss transmission line in recent years [12]-[14]. Owing to the confinement of microwave signals predominantly within the dielectric medium, microwave devices designed based on SIW exhibit inherently low insertion loss and are well-suited for operation at higher frequencies.

This paper presents a novel tri-band bandpass filter based on ( $\lambda_g/4$ ) TSSIRs. The design process is both simple and effective. Conventional  $\lambda_g/4$  uniform impedance resonators, while offering excellent performance, are limited by providing periodic center frequencies for the passbands. By replacing these  $\lambda_g/4$  uniform impedance resonators with  $\lambda_g/4$  TSSIRs, three distinct passbands can be readily achieved. The proposed filter exhibits a compact size, remarkably low insertion loss, and excellent passband symmetry.

Additionally, four inherent transmission zeros within the operational band significantly enhance selectivity and isolation between the three passbands.

## II. ANALYSIS OF TRADITIONAL STUB BANDPASS FILTERS

Traditional stub bandpass filters can be configured in the form illustrated in Fig. 1, which consists of shunt-connected, short-circuited stubs each with an electrical length of  $\theta$  and a characteristic impedance of  $Z_{\rm S}$ , coupled via connecting lines of an electrical length of  $\theta$  and characteristic impedance of  $Z_{\rm T}$ . This particular arrangement leverages the quarter-wavelength resonance principle to achieve selective frequency transmission, effectively attenuating signals outside the designated passband while allowing those within the passband to propagate with minimal loss. Ideal transmission coefficients of the structure shown in Fig. 1 are given in Fig. 2. As depicted in Fig. 2, the stub bandpass filter is designed to exhibit three distinct passbands centered at  $f_0$ ,  $3f_0$ , and  $5f_0$ . These passbands cor-

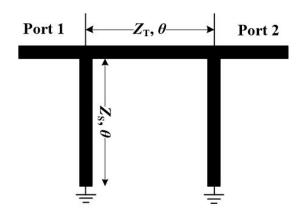


Fig. 1. Transmission line bandpass filter with quarter-wavelength short-circuited stubs.

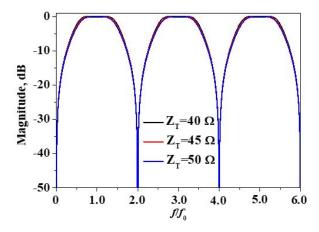


Fig. 2. Simulated transmission coefficients of the structure shown in Fig. 1 with different values of  $Z_T$  ( $Z_S = 50 \,\Omega$ ).

respond to the first three resonant frequencies of the  $\lambda_{\rm g}/4$  uniform impedance resonators employed in the filter design. Additionally, the filter inherently generates four transmission zeros located at DC,  $2f_0$ ,  $4f_0$ , and 6f<sub>0</sub>, respectively. These transmission zeros play a crucial role in enhancing the filter's performance by providing sharp transitions between passbands and stopbands. Consequently, the stub bandpass filter demonstrates superior performance in terms of band-to-band isolation and selectivity. Specifically, the presence of multiple transmission zeros ensures that the filter can effectively attenuate signals outside the desired passbands, thereby minimizing interference and crosstalk between adjacent bands. Simulated transmission coefficients of the structure shown in Fig. 1 with different values of Z<sub>S</sub> are illustrated Fig. 3. As illustrated in Figs. 2 and 3, the transmission characteristics of the stub bandpass filter demonstrate significant stability in response to variations in Z<sub>T</sub>. Specifically, when Z<sub>S</sub> is held constant, the transmission coefficients of the filter remain remarkably consistent, irrespective of fluctuations in Z<sub>T</sub>. This indicates that the filter's performance is relatively insensitive to changes in Z<sub>T</sub> under constant Z<sub>S</sub> conditions. Furthermore, when Z<sub>T</sub> is kept constant, the transmission coefficients of the filter are observed to gradually decrease as the value of Z<sub>S</sub> increases. This suggests that the filter's transmission efficiency is inversely related to the magnitude of Z<sub>S</sub> when Z<sub>T</sub> is maintained at a constant level.

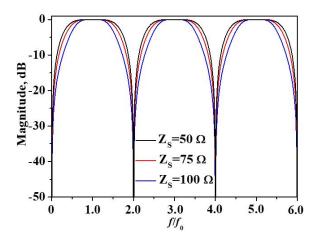


Fig. 3. Simulated transmission coefficients of the structure shown in Fig. 1 with different values of  $Z_S$  ( $Z_T$ =50  $\Omega$ ).

It is worth highlighting that, in contrast to conventional edge-coupled bandpass filters, where bandwidth adjustment is predominantly achieved by varying the widths of the coupling gap, the developed stub bandpass filter exhibits a distinct feature. Specifically, it modulates

its bandwidth by altering the impedance characteristics of the resonator. This unique approach circumvents the potential for spurious losses that typically arise from radiation in the coupling gap of traditional designs. To provide empirical evidence supporting this claim, Fig. 4 illustrates the electric field distributions within the crosssections of both a 50-ohm microstrip transmission line and a 50-ohm coupled transmission line under analogous operating conditions. The electric field distributions of the aforementioned structures were obtained using the relevant functionalities in Ansys HFSS [18]. For both types of structures, namely the 50-ohm microstrip transmission lines and the edge-coupled microstrip lines, the electric field distributions were obtained at an operating frequency of 1 GHz. Upon examination of Fig. 4, it is evident that, when scaled identically, the coupled transmission line exhibits a more pronounced radiation of energy into the surrounding free space. This heightened radiation propensity is inherently associated with increased energy dissipation, thereby resulting in a comparatively higher insertion loss for the entire device. This observation underscores the significance of the design approach adopted in the stub bandpass filter, which effectively mitigates such spurious radiation losses by eschewing reliance on coupling gap adjustments, leading to a more efficient signal transmission and reduced overall insertion loss.

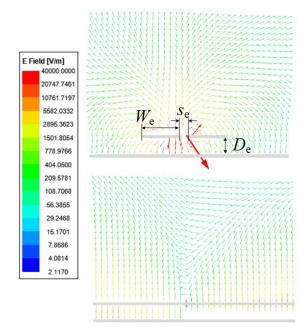


Fig. 4. Electric field distribution on the cross-section of 50-ohm microstrip transmission lines and edge-coupled microstrip lines at 1 GHz ( $W_{\rm e}=1.9$  mm,  $s_{\rm e}=0.2$  mm,  $D_{\rm e}=0.813$  mm).

# III. DESIGN OF THE DEVELOPED TRI-BAND BANDPASS FILTER

# A. Analysis of the $\lambda_g/4$ tri-section stepped impedance resonators (TSSIRs)

The employed  $\lambda_g/4$  TSSIR depicted in Fig. 5 is designed with three distinct characteristic impedances,  $Z_1$ ,  $Z_2$ , and  $Z_3$ . For practical applications, it is advantageous to assume that each section has an equal electrical length. Under this assumption, the input impedances in Fig. 5 can be precisely derived through a series of mathematical transformations:

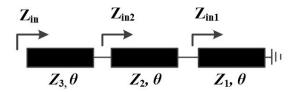


Fig. 5. Structure of  $\lambda_g/4$  TSSIR.

$$Z_{in1} = jZ_1 \tan \theta, \tag{1}$$

$$Z_{in2} = jZ_2 \frac{(Z_1 + Z_2) \tan \theta}{Z_2 - Z_1 \tan^2 \theta},$$
 (2)

$$Z_{in} = jZ_3 \frac{(Z_1 Z_2 + Z_2^2 + Z_1 Z_3) \tan \theta - Z_2 Z_3 \tan^3 \theta}{Z_2 Z_3 - (Z_1 Z_2 + Z_2^2 + Z_1 Z_3) \tan^2 \theta}, \quad (3)$$

while the condition for the first three resonances of this TSSIR can be obtained as:

$$\theta_{01} = \theta = \arctan \sqrt{\frac{K_1 K_2}{1 + K_1 + K_2}},$$
 (4)

$$\theta_{02} = \frac{\pi}{2},\tag{5}$$

$$\theta_{03} = \pi - \theta, \tag{6}$$

where  $K_1 = Z_3/Z_2$ ,  $K_2 = Z_2/Z_1$ . When the discontinuity and dispersion effects of the TSSIR have been ignored, the fundamental property can be obtained as  $f_1 : f_2 : f_3 = \theta_{01} : \theta_{02} : \theta_{03}$ . Therefore, once center frequencies  $f_1, f_2, f_3$  have been assigned, the required impedance ratios for the TSSIR can be determined using the same method as presented in [7].

The locations of transmission zeros of the developed bandpass filter can be determined by setting the input impedance  $Z_{in}$  to zero. This provides the relationship:

$$(Z_1Z_2 + Z_2^2 + Z_1Z_3)\tan\theta = Z_2Z_3\tan^3\theta.$$
 (7)

Solving the above equation yields the following result:

$$\theta_1 = \pi, \tag{8}$$

$$\theta_2 = \arctan(\sqrt{\frac{1 + K_1 + K_2}{K_1 K_2}}),$$
(9)

$$\theta_3 = \pi - \arctan(\sqrt{\frac{1 + K_1 + K_2}{K_1 K_2}}).$$
 (10)

#### B. Tri-band bandpass filter design

Building upon the previous analysis of traditional stub bandpass filters and TSSIRs and drawing parallels to the design methodologies of conventional edge-coupled bandpass filters, the developed tri-band bandpass filter has been designed herein, as illustrated in Fig. 6. In order to minimize the impedance mismatch between the intermediate transmission line and the 50-ohm input/output, the characteristic impedance  $(Z_T)$  of this transmission line between the two resonators was also selected to be 50 ohms.

In this design, the proposed tri-band bandpass filter prototype is designed on a Rogers 4003C substrate  $(\varepsilon_r = 3.55, \tan \delta = 0.0027)$  with a thickness of 0.813 mm. The center frequencies of the three passbands are 1 GHz, 3.5 GHz, and 6 GHz. Referring to the above theoretical analysis described in section II, the impedance ratios can be found to be  $K_1 = 0.75$  and  $K_2 = 0.66$ . The width of the middle section of the proposed  $\lambda_g/4$  TSSIR is selected as 2 mm, which corresponds to a characteristic impedance of 46  $\Omega$ . The characteristic impedances of the other two sections are calculated to be  $Z_1 = 70 \Omega$  and  $Z_2 = 35 \Omega$ . Meanwhile, the electric length of each section at 1 GHz can be calculated as  $\theta = \theta_{01} = \theta_{02} = \theta_{03} = 25.7^{\circ}$ . Layout of the developed tri-band bandpass filter based on  $\lambda_g/4$  TSSIRs is given in Fig. 7. For demonstration, cur-

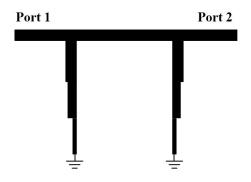


Fig. 6. Proposed tri-band bandpass filter based on  $\lambda_g/4$  TSSIRs.

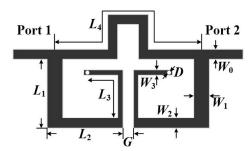


Fig. 7. Layout of the developed tri-band bandpass filter based on  $\lambda_g/4$  TSSIRs.

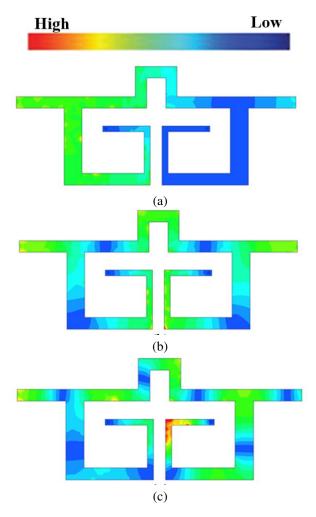


Fig. 8. Current distributions at center frequencies of three passbands: (a) first passband (1 GHz), (b) second passband (3.5 GHz), (c) third passband (6 GHz).

rent distributions at center frequencies of three passbands are shown in Fig. 8.

#### IV. RESULTS AND DISCUSSION

A photograph of the fabricated tri-band bandpass filter is depicted in Fig. 9, while the pertinent parameters of the tri-band filter are also provided. A comprehensive comparison between the simulated and measured results of the proposed tri-band bandpass filter is illustrated in Figs. 10 and 11. Additionally, the measured group delay of the filter is presented in Fig. 12. The filter exhibits three distinct passbands centered at 1 GHz, 3.5 GHz, and 6 GHz, respectively. Leveraging the aforementioned advantageous characteristics of the conventional filter structure, the measured minimum insertion losses of the three passbands are 0.07 dB, 0.52 dB, and 1.14 dB, respectively, inclusive of the losses attributed to the SMA connectors. Notably, the transmission zeros gener-

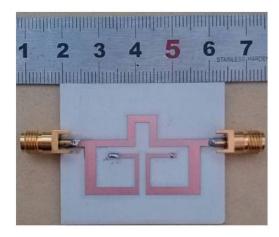


Fig. 9. Photograph of the proposed tri-band bandpass filter ( $W_0 = 1.9 \text{ mm}$ ,  $W_1 = 3.05 \text{ mm}$ ,  $W_2 = 2 \text{ mm}$ ,  $W_3 = 1 \text{ mm}$ ,  $L_1 = 13 \text{ mm}$ ,  $L_2 = 14.5 \text{ mm}$ ,  $L_3 = 14 \text{ mm}$ ,  $L_4 = 41.2 \text{ mm}$ , D = 0.6 mm, G = 2 mm).

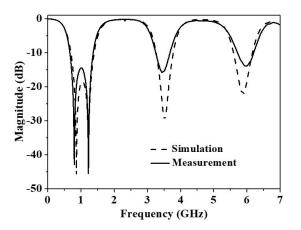


Fig. 10. Simulated and measured reflection coefficients of the developed tri-band bandpass filter.

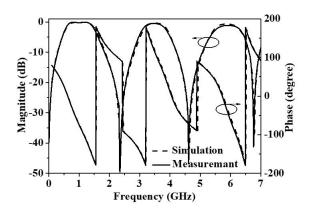


Fig. 11. Simulated and measured transmission coefficients and phase of the developed tri-band bandpass filter.

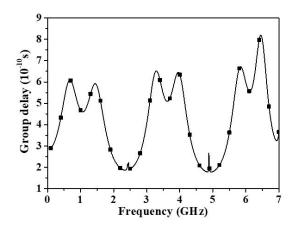


Fig. 12. Measured group delay versus frequency for each passband.

ated at 0 GHz, 2.35 GHz, 4.6 GHz, and 6.75 GHz have significantly enhanced the selectivity, passband symmetry, and band-to-band isolation of the proposed tri-band filter.

In order to comprehensively verify the accuracy of the transmission zero formulas that were derived in the previous section, a detailed comparison was conducted between the calculated values and those obtained through both simulation and experimental measurement. The results of this comparison are presented in Table 1. The calculated transmission zero locations exhibit a high degree of alignment with the measured results, effectively demonstrating the validity and reliability of the design methodology employed in this study.

For a bandpass filter, the passband symmetry can be quantified as follows. As shown in Fig. 13, the center frequency of the filter is f, the lower passband edge corresponding to the -10 dB level is  $f_{\rm L}$ , and the upper passband edge corresponding to the -10 dB level is  $f_{\rm H}$ . For an ideal bandpass filter, the symmetry condition can be

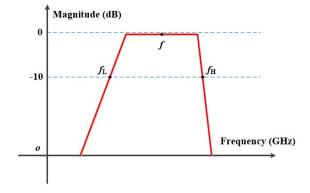


Fig. 13. Transmission coefficient of a bandpass filter.

Table 1: Calculated and measured locations of transmission zeros

	1	2	3	4
Calculated Results	0 GHz	2.32 GHz	4.69 GHz	7.0 GHz
Measured Results	0 GHz	2.55 GHz	4.45 GHz	6.75 GHz

Table 2: Comparison between proposed tri-band filter and prior works

4	f <sub>0</sub> /f <sub>1</sub> /f <sub>2</sub> GHz 2.5/3.5/5.7	<b>dB</b> 1 / 1.2 / 1.5	Process  Microstrip	Passband Symmetry Ratio	$oldsymbol{\lambda}_g{ imes}oldsymbol{\lambda}_g^*$
4		1 / 1.2 / 1.5	Microstrip		
			wherosurp	1.6/1.06/1.18	$0.26 \times 0.2$
			line		
5	1.84/2.45/2.98	0.9/1.6/0.8	Microstrip	1.1/1/14/1.5	$0.27 \times 0.2$
			line		
6	1.8/3.5/5.8	0.88/1.33/1.77	Microstrip	1.1/1.04/1.52	$0.52 \times 0.11$
			line		
7	1.57 / 2.45 / 3.5	0.77/1.51/1/8	Microstrip	1.13/1.14/1.2	$0.23 \times 0.16$
			line		
8	1.0 / 2.4 / 2.6	2.0 / 1.9 / 1.7	Microstrip	1.7/1.07/1.06	0.2×0.2
			line		
9	1.64 / 3.04 / 4.8	1.54 / 1.71 / 2.4**	Microstrip	1.14/1.18/1.75	$0.24 \times 0.2$
			line		
10	3.16 / 4.27 / 5.70	1.6 / 2.5 / 2.9	Microstrip	1.1/1.05/1.64	$0.59 \times 0.19$
			line		
11	1.15 / 2.05 / 3.18	0.92 / 0.93 / 1.58	Microstrip	1.74/1.13/1.3	NA
			line		
12	3.01 / 3.34 / 3.58	1.71 / 1.58 / 1.13	SIW	1.62/1.5/1.5	$0.58 \times 0.21$
13	3.02 / 4.23 / 5.31	3.14 / 2.32 / 3.21	SIW	1.28/1.26/1/24	$1.45 \times 0.74$
14	14.08 / 14.51 / 14.86	2.55 / 2.71 / 2.03	SIW	1.5/1.1/1.7	1.64×1.55
15	1.72 / 4.05 / 7.6	0.13 / 0.15 / 0.21	Microstrip	1.3/1.27/1.67	$0.19 \times 0.11$
			line ***		
16	1.56 / 4.21 / 5.79	0.18 / 0.19 / 0.18	Microstrip	1.1./1/13/1.21	$0.26 \times 0.15$
			line ***		
17	1.64 / 2.48 / 3.51	0.051 / 0.09 / 0.12	Microstrip	1.3/1.15/1.28	$0.19 \times 0.16$
			line ***		
This	1/3.5/6	0.07 / 0.52/ 1.14	Microstrip	1.19/1.07/1.03	$0.17 \times 0.12$
Work			line		

<sup>\*</sup>  $\lambda_g$  is the guided wavelength at the center frequency of the first passband  $(f_1)$ .

expressed as  $f_H$ -f=f- $f_L$ , and passband symmetry ratio (r) which can be expressed as r= $(f_H$ -f)/(f- $f_L)$ =1. This metric provides a clear and quantitative measure of the passband symmetry.

However, for commonly used bandpass filters, it is challenging to achieve r=1. Except, the closer the value of r is to 1, the better the passband symmetry of the filter. Therefore, we define the passband symmetry ratio r as:

$$r = \frac{\max[(f_{\rm H} - f), (f - f_{\rm L})]}{\min[(f_{\rm H} - f), (f - f_{\rm L})]}.$$
 (11)

Under this definition, the value of r is always greater than 1, which facilitates comparison.

For a more thorough evaluation, comparisons with prior works are presented in Table 1. As seen from Table 1, compared with conventional microstrip tri-band filters, the proposed design demonstrates significantly lower insertion loss while maintaining comparable circuit dimensions. Furthermore, when juxtaposed with triband filters based on SIW structures, the filter presented in this work exhibits certain advantages in both insertion loss and circuit size. Moreover, Table 1 also includes triband filters based on high-temperature superconducting (HTS) structures [15]–[17]. The aforementioned filters are similarly designed using edge-coupled structures. In terms of insertion loss, the first two passbands of the proposed tri-band filter in this work still exhibit comparable

<sup>\*\*</sup> Only simulated results have been given in this design.

<sup>\*\*\*</sup> These designs are based on HTS.

performance with those of HTS-based filters. As shown in Table 1, for the three bandpass filters designed in this paper, the passband symmetry ratio for each passband is less than 1.2, indicating that the design exhibits good passband symmetry.

In summary, the developed filter offers several advantages. Firstly, it employs a  $\lambda_g/4$  TSSIR resonator, which significantly reduces the overall dimensions of the filter compared to existing ones. Secondly, the adoption of a non-edge-coupled structure effectively avoids radiation losses caused by coupling slots, resulting in a low insertion loss, a crucial characteristic for microwave passive devices. Lastly, due to the inherent characteristics of the structure, the single passband of the filter exhibits good symmetry, which is closer to that of an ideal bandpass filter.

#### V. CONCLUSION

This paper introduces a microstrip line-based triband bandpass filter employing quarter-wavelength trisection stepped impedance resonators (TSSIR). The design process of the proposed filter is characterized by its simplicity and effectiveness. By judiciously adjusting the impedance values of the TSSIR, three distinct passbands can be readily achieved, thus catering to the requirements of multi-band applications. The inherent generation of transmission zeros within the entire operating bandwidth significantly enhances the selectivity, passband symmetry, and band-to-band isolation of the proposed tri-band filter. The consistency between the simulated and measured results further validates the feasibility of the design. These attributes collectively render the filter highly suitable for modern compact tri-band communication systems.

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